

Università degli studi di Roma la Sapienza

Meccanica applicata alle macchine per
gli allievi del corso di Ingegneria Meccanica
A.A. 2008 - 2009

METODO ANALITICO ESATTO

RIEPILOGO DELLE FORMULE USATE

Materiale di supporto per l'esercitazione

$$\omega_4 := \frac{\omega_2 r_2 \sin(\theta_2 - \theta_3)}{r_4 \sin(-\theta_4 + \theta_3)}$$

$$\omega_3 := - \frac{\omega_2 r_2 \sin(\theta_2 - \theta_4)}{r_3 \sin(-\theta_4 + \theta_3)}$$

$$\alpha_4 := \frac{\alpha_2 r_2 \sin(\theta_2 - \theta_3) + \omega_2^2 r_2 \cos(\theta_2 - \theta_3) + \frac{\omega_2^2 r_2^2 \sin(\theta_2 - \theta_4)^2}{r_3 \sin(-\theta_4 + \theta_3)^2} + \frac{\omega_2^2 r_2^2 \sin(\theta_2 - \theta_3)^2 \cos(-\theta_4 + \theta_3)}{r_4 \sin(-\theta_4 + \theta_3)^2}}{r_4 \sin(-\theta_4 + \theta_3)}$$

$$\alpha_3 := - \frac{\alpha_2 r_2 \sin(\theta_2 - \theta_4) + \omega_2^2 r_2 \cos(\theta_2 - \theta_4) + \frac{\omega_2^2 r_2^2 \sin(\theta_2 - \theta_3)^2}{r_4 \sin(-\theta_4 + \theta_3)^2} + \frac{\omega_2^2 r_2^2 \sin(\theta_2 - \theta_4)^2 \cos(-\theta_4 + \theta_3)}{r_3 \sin(-\theta_4 + \theta_3)^2}}{r_3 \sin(-\theta_4 + \theta_3)}$$

Analisi cinematica del quadrilatero articolato

Analisi delle posizioni per un assegnato angolo dell'asta movente

r1 = telaio

r2 = asta movente

r3 = biella

r4 = asta cedente (bilanciere o manovella)

$$\theta_1 := \pi$$

$$chiusura_1 := -r_1 + r_2 \cos(\theta_2) + r_3 \cos(\theta_3) + r_4 \cos(\theta_4) = 0$$

$$chiusura_2 := r_2 \sin(\theta_2) + r_3 \sin(\theta_3) + r_4 \sin(\theta_4) = 0$$

$$equaz = -r_3^2 + (r_1 - r_2 \cos(\theta_2) - r_4 \cos(\theta_4))^2 + (-r_2 \sin(\theta_2) - r_4 \sin(\theta_4))^2$$

$$equaz = -r_3^2 + r_1^2 - 2 r_1 r_2 \cos(\theta_2) - 2 r_1 r_4 \cos(\theta_4) + 2 r_2 \cos(\theta_2) r_4 \cos(\theta_4) + r_2^2 + 2 r_2 \sin(\theta_2) r_4 \sin(\theta_4) + r_4^2$$

$$equaz1 = (2 r_2 \cos(\theta_2) r_4 - 2 r_1 r_4) \cos(\theta_4) - r_3^2 + r_1^2 - 2 r_1 r_2 \cos(\theta_2) + r_4^2 + r_2^2 + 2 r_2 \sin(\theta_2) r_4 \sin(\theta_4)$$

$$A := 2 r_2 \cos(\theta_2) r_4 - 2 r_1 r_4$$

$$B := 2 r_2 \sin(\theta_2) r_4$$

$$C := -r_3^2 + r_1^2 - 2 r_1 r_2 \cos(\theta_2) + r_4^2 + r_2^2$$

$$\theta_2 := 0.3490658504$$

$$\omega_2 := 41.88790204$$

$$\alpha_2 := 0$$

$$t_2 := 0.3490658504$$

$$r_1 := 80$$

$$r_2 := 20$$

$$r_3 := 50$$

$$r_4 := 70$$

$$(2800. \cos(\theta_2) - 11200.) \cos(\theta_4) + 9200. - 3200. \cos(\theta_2) + 2800. \sin(\theta_2) \sin(\theta_4)$$

$$equaz2 = \frac{(2800 \cos(\theta_2) - 11200) (1 - t_2^2)}{1 + t_2^2} + 9200 - 3200 \cos(\theta_2) + 2800 \sin(\theta_2) \sin(\theta_4)$$

$$equaz3 = \frac{(2800 \cos(\theta_2) - 11200) (1 - t_2^2)}{1 + t_2^2} + 9200 - 3200 \cos(\theta_2) + \frac{5600 \sin(\theta_2) t_2}{1 + t_2^2}$$

soluzioni:=

$$\frac{1}{2 \left(75 \sin(\theta_2)^2 + 792 \right)} \left(-70 \sin(\theta_2) \cos(\theta_2) - 238 \sin(\theta_2) \right. \\ \left. + 2 \sqrt{\left((2800 \cos(\theta_2) - 11200)^2 (1 - t_2^2)^2 + (9200 - 3200 \cos(\theta_2) + 2800 \sin(\theta_2) \sin(\theta_4))^2 \right)} \right)$$

$$\begin{aligned}
 & 1225 \sin(\theta_2)^2 \cos(\theta_2)^2 + 11480 \sin(\theta_2)^2 \cos(\theta_2) + 16951 \sin(\theta_2)^2 - 375 \sin(\theta_2)^4 + 71280 \\
 & + 33264 \cos(\theta_2) \Big) \Big), \\
 & \frac{1}{2 \left(75 \sin(\theta_2)^2 + 792 \right)} \left(-70 \sin(\theta_2) \cos(\theta_2) - 238 \sin(\theta_2) \right. \\
 & \left. - 2 \sqrt{1225 \sin(\theta_2)^2 \cos(\theta_2)^2 + 11480 \sin(\theta_2)^2 \cos(\theta_2) + 16951 \sin(\theta_2)^2 - 375 \sin(\theta_2)^4 + 71280} \right. \\
 & \left. + 33264 \cos(\theta_2) \right) \Big)
 \end{aligned}$$

tang_theta_4_mezzi:1

$$\frac{35 \sin(\theta_2) \cos(\theta_2) + 119 \sin(\theta_2) - 2 \sqrt{2} \sqrt{-\left(8 \cos(\theta_2)^2 + 3 \cos(\theta_2) - 38 \right) (5 \cos(\theta_2) + 17)^2}}{3 \left(-289 + 25 \cos(\theta_2)^2 \right)}$$

tang_theta_4_mezzi:2

$$\frac{35 \sin(\theta_2) \cos(\theta_2) + 119 \sin(\theta_2) + 2 \sqrt{2} \sqrt{-\left(8 \cos(\theta_2)^2 + 3 \cos(\theta_2) - 38 \right) (5 \cos(\theta_2) + 17)^2}}{3 \left(-289 + 25 \cos(\theta_2)^2 \right)}$$

Inizio della procedura di calcolo PER IL QUADRILATERO

$$\cos_t3 = \frac{8}{5} - \frac{2}{5} \cos(\theta_2) - \frac{7}{5} \cos(\theta_4)$$

$$\sin_t3 = -\frac{2}{5} \sin(\theta_2) - \frac{7}{5} \sin(\theta_4)$$

$$\textit{tang_t4_mezzi_1} = 0.3415198560$$

$$\textit{t4_1} = 0.6582004832$$

$$\textit{ct3_1} = 0.116590980$$

$$\textit{st3_1} = -.9931800153$$

$$\textit{tang_t4_mezzi_2} = -.4712673840$$

$t4_2 := -.8807969084$
 $ct3_2 := 0.3329715248$
 $st3_2 := 0.9429368817$

VALORI NUMERICI

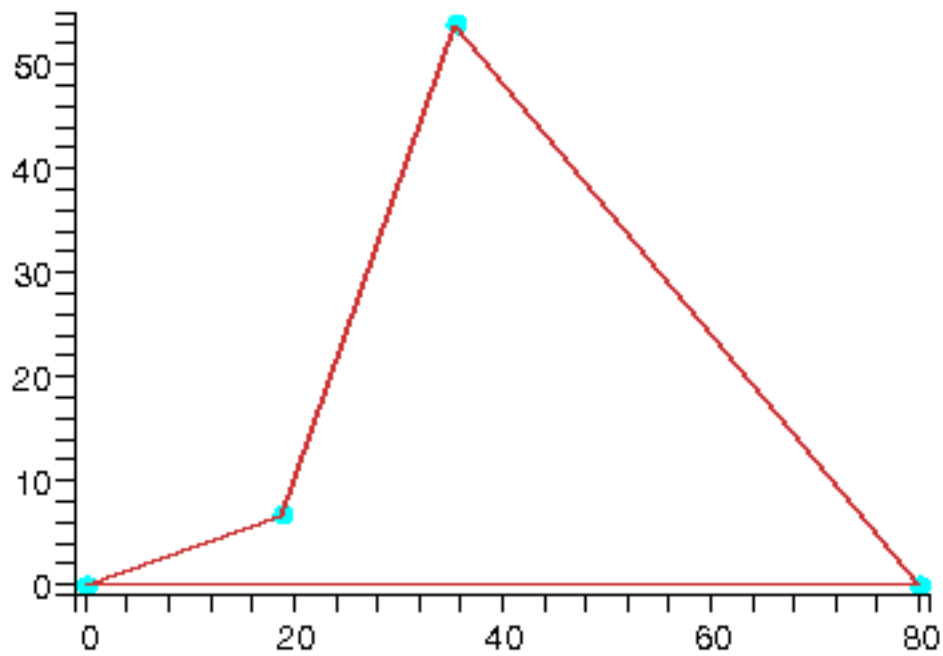
70.55076539
 $t3 := 1.231343146$
 0
 $\omega4 := -10.78335923$
 $\omega3 := -18.42528424$
 $\alpha4 := 584.7107578$
 $\alpha3 := -259.6554635$

$I_1 := 80$
 $I_2 := 20$
 $I_3 := 50$
 $I_4 := 70$

GRAFICO DEL QUADRILATERO

Warning, the previous binding of the name CrossProduct has been removed and it now has an assigned value

$rag_cer := 1$
 $quadri := \{\}$
 $Ax := 0$
 $Ay := 0$
 $Bx := 18.79385242$
 $By := 6.840402866$
 $Cx := 35.44242866$
 $Cy := 53.98724695$
 $Dx := 80$
 $Dy := 0$



Individuazione del quadrilatero articolato (ovvero degli infiniti quadrilateri articolati)

20.00000000

49.99999998

69.99999998

80.00000000

G2

G3

G4

name of the object: CP form of the object: point2d coordinates of the point: [35.44242866, 53.987

name of the object: G2 form of the object: point2d coordinates of the point: [9.396926210, 3.4202

$$PG2 := \begin{bmatrix} 9.396926210 \\ 3.420201433 \end{bmatrix}$$

$$\Omega_2 := \begin{bmatrix} 0 & -41.88790204 \\ 41.88790204 & 0 \end{bmatrix}$$

$$VG2 := \begin{bmatrix} -143.265062582571630 \\ 393.617524561588482 \end{bmatrix}$$

$$\Omega_3 := \begin{bmatrix} 0 & 18.42528424 \\ -18.42528424 & 0 \end{bmatrix}$$

$$PB := \begin{bmatrix} 18.7938524200000004 \\ 6.84040286599999980 \end{bmatrix}$$

$$BG3x := 8.324288150$$

$$BG3y := 23.57342204$$

$$BG3 := \begin{bmatrix} 8.324288150 \\ 23.57342204 \end{bmatrix}$$

$$PG3 := \begin{bmatrix} 27.1181405700000013 \\ 30.4138249060000021 \end{bmatrix}$$

$$VG3_B := \begin{bmatrix} 434.347001596480652 \\ -153.377375259413753 \end{bmatrix}$$

$$VB := \begin{bmatrix} -286.530125165143260 \\ 787.235049123176964 \end{bmatrix}$$

$$VG3 := \begin{bmatrix} 147.816876431337392 \\ 633.857673863763239 \end{bmatrix}$$

$$VC := \begin{bmatrix} 582.163878027818100 \\ 480.480298604349457 \end{bmatrix}$$

$$PC := \begin{bmatrix} 35.4424287199999953 \\ 53.9872469459999990 \end{bmatrix}$$

$$CG4x := 22.27878568$$

$$CG4y := -26.99362348$$

$$CG4 := \begin{bmatrix} 22.27878568 \\ -26.99362348 \end{bmatrix}$$

$$PG4:=\begin{bmatrix} 57.7212143999999938 \\ 26.9936234659999990 \end{bmatrix}$$

$$\Omega_4:=\begin{bmatrix} & 0 & 10.78335923 \\ -10.78335923 & & 0 \end{bmatrix}$$

$$VG4_C:=\begin{bmatrix} -291.081938904202730 \\ -240.240149195619807 \end{bmatrix}$$

$$VG4:=\begin{bmatrix} 291.081939123615371 \\ 240.240149408729650 \end{bmatrix}$$

$$scala_V:= 0.02$$

$$ext_V2_x= 6.531624958$$

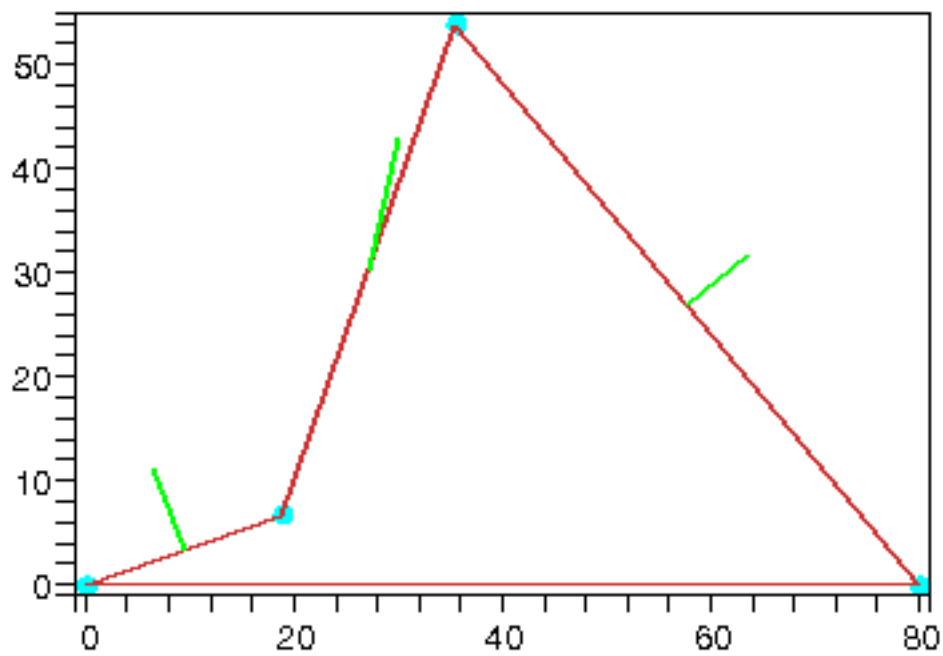
$$ext_V2_y= 11.29255192$$

$$ext_V3_x= 30.07447810$$

$$ext_V3_y= 43.09097839$$

$$ext_V4_x= 63.54285318$$

$$ext_V4_y= 31.79842646$$



$$A2 := \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$A3 := \begin{bmatrix} 0 & 259.6554635 \\ -259.6554635 & 0 \end{bmatrix}$$

$$A4 := \begin{bmatrix} 0 & -584.7107578 \\ 584.7107578 & 0 \end{bmatrix}$$

$$\text{scala_A} = 0.0005$$

$$AG2 := \begin{bmatrix} -16487.8123100631128 \\ -6001.07290721322988 \end{bmatrix}$$

$$\text{ext_A2_x} = 1.153020055$$

$$\text{ext_A2_y} = 0.419664979$$

EA2P

AcG2

$$AcB:=\begin{bmatrix} -32975.6246201262256 \\ -12002.1458144264598 \end{bmatrix}$$

$$AG3:=\begin{bmatrix} -29680.6785291887500 \\ -22166.5596755291590 \end{bmatrix}$$

$$AcC:=\begin{bmatrix} -26385.7324382512816 \\ -32330.9735366318564 \end{bmatrix}$$

$$ext_A3_x= 12.27780131$$

$$ext_A3_y= 19.33054507$$

EA3P

AcG3

$$DG4:=\begin{bmatrix} -22.27878560000000062 \\ 26.99362346599999990 \end{bmatrix}$$

$$AG4:=\begin{bmatrix} -13192.8662116300257 \\ -16165.4867219807311 \end{bmatrix}$$

$$ext_A4_x= 51.12478130$$

$$ext_A4_y= 18.91088011$$

EA4P

AcG4

